

$$\begin{aligned} \text{f) } \quad & \frac{1}{2}x^2 + 3x - 6 = 0 \\ & \frac{1}{2}(x^2 + 6x) - 6 = 0 \\ & \frac{1}{2}(x^2 + 6x + 9 - 9) - 6 = 0 \\ & \frac{1}{2}(x + 3)^2 - \frac{9}{2} - 6 = 0 \\ & \frac{1}{2}(x + 3)^2 - \frac{21}{2} = 0 \end{aligned}$$

Section 4.3 Page 240 Question 4

$$\begin{aligned} \text{a) } \quad & x^2 = 64 \\ & x = \pm 8 \end{aligned}$$

$$\begin{aligned} \text{b) } \quad & 2s^2 - 8 = 0 \\ & 2s^2 = 8 \\ & s = \pm 2 \end{aligned}$$

$$\begin{aligned} \text{c) } \quad & \frac{1}{3}t^2 - 1 = 11 \\ & \frac{1}{3}t^2 = 12 \\ & t^2 = 36 \\ & t = \pm 6 \end{aligned}$$

$$\begin{aligned} \text{d) } \quad & -y^2 + 5 = -6 \\ & y^2 = 11 \\ & y = \pm\sqrt{11} \end{aligned}$$

Section 4.3 Page 241 Question 5

$$\begin{aligned} \text{a) } \quad & (x - 3)^2 = 4 \\ & x - 3 = \pm 2 \\ & x = 3 \pm 2 \\ x = 3 + 2 \quad & \text{or} \quad x = 3 - 2 \\ x = 5 \quad & \quad \quad x = 1 \end{aligned}$$

$$\begin{aligned} \text{b) } \quad & (x + 2)^2 = 9 \\ & x + 2 = \pm 3 \\ & x = -2 \pm 3 \\ x = -2 + 3 \quad & \text{or} \quad x = -2 - 3 \\ x = 1 \quad & \quad \quad x = -5 \end{aligned}$$

$$\begin{aligned} \text{c) } \quad & \left(d + \frac{1}{2}\right)^2 = 1 \\ & d + \frac{1}{2} = \pm 1 \\ & d = -\frac{1}{2} \pm 1 \\ d = -\frac{1}{2} + 1 \quad & \text{or} \quad d = -\frac{1}{2} - 1 \\ d = \frac{1}{2} \quad & \quad \quad d = -\frac{3}{2} \end{aligned}$$

$$\begin{aligned} \text{d) } \quad & \left(h - \frac{3}{4}\right)^2 = \frac{7}{16} \\ & h - \frac{3}{4} = \pm\sqrt{\frac{7}{16}} \\ & h = \frac{3}{4} \pm \frac{\sqrt{7}}{4} \\ & h = \frac{3 \pm \sqrt{7}}{4} \end{aligned}$$

$$\text{e) } (s + 6)^2 = \frac{3}{4}$$

$$s + 6 = \pm\sqrt{\frac{3}{4}}$$

$$s = -6 \pm \frac{\sqrt{3}}{2}$$

$$s = \frac{-12 \pm \sqrt{3}}{2}$$

$$\text{f) } (x + 4)^2 = 18$$

$$x + 4 = \pm\sqrt{18}$$

$$x = -4 \pm 3\sqrt{2}$$

Section 4.3 Page 241 Question 6

$$\text{a) } x^2 + 10x + 4 = 0$$

$$x^2 + 10x = -4$$

$$x^2 + 10x + 25 = -4 + 25$$

$$(x + 5)^2 = 21$$

$$x + 5 = \pm\sqrt{21}$$

$$x = -5 \pm \sqrt{21}$$

$$\text{b) } x^2 - 8x + 13 = 0$$

$$x^2 - 8x = -13$$

$$x^2 - 8x + 16 = -13 + 16$$

$$(x - 4)^2 = 3$$

$$x - 4 = \pm\sqrt{3}$$

$$x = 4 \pm \sqrt{3}$$

$$\text{c) } 3x^2 + 6x + 1 = 0$$

$$x^2 + 2x + \frac{1}{3} = 0$$

$$x^2 + 2x = -\frac{1}{3}$$

$$x^2 + 2x + 1 = -\frac{1}{3} + 1$$

$$(x + 1)^2 = \frac{2}{3}$$

$$x + 1 = \pm\sqrt{\frac{2}{3}}$$

$$x = -1 \pm \frac{\sqrt{6}}{3}$$

$$x = \frac{-3 \pm \sqrt{6}}{3}$$

$$\text{d) } -2x^2 + 4x + 3 = 0$$

$$x^2 - 2x - \frac{3}{2} = 0$$

$$x^2 - 2x = \frac{3}{2}$$

$$x^2 - 2x + 1 = \frac{3}{2} + 1$$

$$(x - 1)^2 = \frac{5}{2}$$

$$x - 1 = \pm\sqrt{\frac{5}{2}}$$

$$x = 1 \pm \frac{\sqrt{10}}{2}$$

$$x = \frac{2 \pm \sqrt{10}}{2}$$

$$\begin{aligned}
 \text{e) } -0.1x^2 - 0.6x + 0.4 &= 0 \\
 x^2 + 6x - 4 &= 0 \\
 x^2 + 6x &= 4 \\
 x^2 + 6x + 9 &= 4 + 9 \\
 (x + 3)^2 &= 13 \\
 x + 3 &= \pm\sqrt{13} \\
 x &= -3 \pm \sqrt{13}
 \end{aligned}$$

$$\begin{aligned}
 \text{f) } 0.5x^2 - 4x - 6 &= 0 \\
 x^2 - 8x - 12 &= 0 \\
 x^2 - 8x &= 12 \\
 x^2 - 8x + 16 &= 12 + 16 \\
 (x - 4)^2 &= 28 \\
 x - 4 &= \pm\sqrt{28} \\
 x &= 4 \pm 2\sqrt{7}
 \end{aligned}$$

Section 4.3 Page 241 Question 7

$$\begin{aligned}
 \text{a) } x^2 - 8x - 4 &= 0 \\
 x^2 - 8x &= 4 \\
 x^2 - 8x + 16 &= 4 + 16 \\
 (x - 4)^2 &= 20 \\
 x - 4 &= \pm\sqrt{20} \\
 x - 4 = \sqrt{20} \quad \text{or} \quad x - 4 &= -\sqrt{20} \\
 x = 4 + \sqrt{20} \quad \quad \quad x &= 4 - \sqrt{20} \\
 x \approx 8.5 \quad \quad \quad x &\approx -0.5
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } -3x^2 + 4x + 5 &= 0 \\
 x^2 - \frac{4}{3}x &= \frac{5}{3} \\
 x^2 - \frac{4}{3}x + \frac{4}{9} &= \frac{5}{3} + \frac{4}{9} \\
 \left(x - \frac{2}{3}\right)^2 &= \frac{19}{9} \\
 x - \frac{2}{3} &= \pm\sqrt{\frac{19}{9}} \\
 x &= \frac{2 \pm \sqrt{19}}{3} \\
 x = \frac{2 + \sqrt{19}}{3} \quad \text{or} \quad x &= \frac{2 - \sqrt{19}}{3} \\
 x \approx 2.1 \quad \quad \quad x &\approx -0.8
 \end{aligned}$$

$$\text{c) } \frac{1}{2}x^2 - 6x - 5 = 0$$

$$x^2 - 12x = 10$$

$$x^2 - 12x + 36 = 10 + 36$$

$$(x - 6)^2 = 46$$

$$x - 6 = \pm\sqrt{46}$$

$$x - 6 = \sqrt{46} \quad \text{or} \quad x - 6 = -\sqrt{46}$$

$$x = 6 + \sqrt{46} \quad x = 6 - \sqrt{46}$$

$$x \approx 12.8 \quad x \approx -0.8$$

$$\text{d) } 0.2x^2 + 0.12x - 11 = 0$$

$$x^2 + 0.6x = 55$$

$$x^2 + 0.6x + 0.09 = 55 + 0.09$$

$$(x + 0.3)^2 = 55.09$$

$$x + 0.3 = \pm\sqrt{55.09}$$

$$x + 0.3 = \sqrt{55.09} \quad \text{or} \quad x + 0.3 = -\sqrt{55.09}$$

$$x = -0.3 + \sqrt{55.09} \quad x = -0.3 - \sqrt{55.09}$$

$$x \approx 7.1 \quad x \approx -7.7$$

$$\text{e) } -\frac{2}{3}x^2 - x + 2 = 0$$

$$x^2 + \frac{3}{2}x = 3$$

$$x^2 + \frac{3}{2}x + \frac{9}{16} = 3 + \frac{9}{16}$$

$$\left(x + \frac{3}{4}\right)^2 = \frac{57}{16}$$

$$x + \frac{3}{4} = \pm\sqrt{\frac{57}{16}}$$

$$x = \frac{-3 \pm \sqrt{57}}{4}$$

$$x = \frac{-3 + \sqrt{57}}{4} \quad \text{or} \quad x = \frac{-3 - \sqrt{57}}{4}$$

$$x \approx 1.1 \quad x \approx -2.6$$

$$\text{f) } \frac{3}{4}x^2 + 6x + 1 = 0$$

$$x^2 + 8x = -\frac{4}{3}$$

$$x^2 + 8x + 16 = -\frac{4}{3} + 16$$

$$(x + 4)^2 = \frac{44}{3}$$

$$x + 4 = \pm\sqrt{\frac{44}{3}}$$

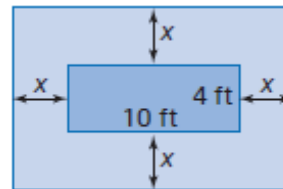
$$x + 4 = \sqrt{\frac{44}{3}} \quad \text{or} \quad x + 4 = -\sqrt{\frac{44}{3}}$$

$$x = -4 + \sqrt{\frac{44}{3}} \quad x = -4 - \sqrt{\frac{44}{3}}$$

$$x \approx -0.2 \quad x \approx -7.8$$

Section 4.3 Page 241 Question 8

a) Let x represent the distance added to each side of the kennel.



b) An equation that models the new area is $80 = (4 + 2x)(10 + 2x)$ or $0 = 4x^2 + 28x - 40$.

$$\text{c) } 4x^2 + 28x - 40 = 0$$

$$x^2 + 7x = 10$$

$$x^2 + 7x + \frac{49}{4} = 10 + \frac{49}{4}$$

$$\left(x + \frac{7}{2}\right)^2 = \frac{89}{4}$$

$$x + \frac{7}{2} = \pm\sqrt{\frac{89}{4}}$$

$$x = \frac{-7 \pm \sqrt{89}}{2}$$

$$x = \frac{-7 + \sqrt{89}}{2} \quad \text{or} \quad x = \frac{-7 - \sqrt{89}}{2}$$

$$x \approx 1.2$$

$$x \approx -8.2$$

Since the distance added to the kennel cannot be negative, $x = -8.2$ is an extraneous root.

The dimensions of the new kennel are $4 + 2(1.2)$, or 6.4 ft, by $10 + 2(1.2)$, or 12.4 ft.