

Section 2.3 Page 108 Question 6

a) Given $\angle A = 39^\circ$, $a = 10$ cm, and $b = 14$ cm:

$$b \sin A = 14 \sin 39^\circ$$

$$b \sin A = 8.810\dots$$

Then, $b \sin A < a < b$ so there are two solutions.

b) Given $\angle A = 123^\circ$, $a = 23$ cm, and $b = 12$ cm:

$\angle A$ is obtuse and $a > b$ so there is one solution.

c) Given $\angle A = 145^\circ$, $a = 18$ cm, and $b = 10$ cm:

$\angle A$ is obtuse and $a > b$ so there is one solution.

d) Given $\angle A = 124^\circ$, $a = 1$ cm, and $b = 2$ cm:

$\angle A$ is obtuse and $a < b$ so there is no solution.

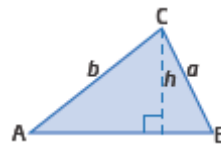
Section 2.3 Page 108 Question 7

a) $\sin A = \frac{h}{b}$

$$h = b \sin A$$

Then, from the diagram, $a > b \sin A$, or

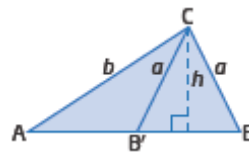
$a > h$ and $b > h$.



b) $\sin A = \frac{h}{b}$

$$h = b \sin A$$

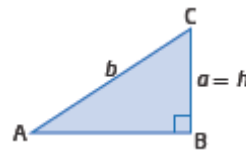
Then, from the diagram, $b \sin A < a < b$.



c) $\sin A = \frac{h}{b}$

$$h = b \sin A$$

Also, from the diagram, $a = b \sin A$.



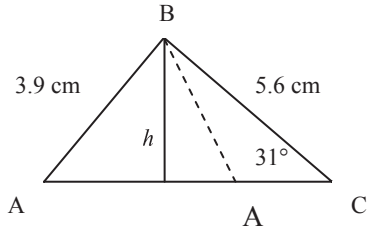
d) $\sin A = \frac{h}{b}$

$$h = b \sin A$$

From the diagram, $a \geq b > b \sin A$.

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a) The diagram shows the given information.
 This is an ambiguous case, since $h = 5.6 \sin 31^\circ = 2.884\dots$
 Because h is less than 5.6 and 3.9, two solutions are possible.



$$\frac{\sin A}{5.6} = \frac{\sin 31^\circ}{3.9}$$

$$\sin A = \frac{5.6 \sin 31^\circ}{3.9}$$

$$\angle A = \sin^{-1}\left(\frac{5.6 \sin 31^\circ}{3.9}\right)$$

$$\angle A = 47.692\dots$$

Or, $\angle A = 180^\circ - 47.692\dots^\circ$
 $\angle A = 132.308\dots^\circ$

$$\angle B = 180^\circ - (31^\circ + 48^\circ) \quad \text{or} \quad \angle B = 180^\circ - (31^\circ + 132^\circ)$$

$$\angle B = 101^\circ \quad \quad \quad \angle B = 17^\circ$$

Determine b for each measure of $\angle B$:

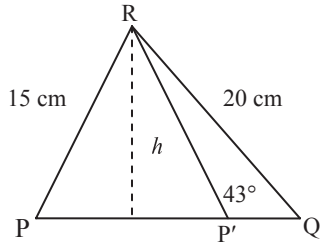
$$\frac{b}{\sin 101^\circ} = \frac{3.9}{\sin 31^\circ} \quad \quad \quad \frac{b}{\sin 17^\circ} = \frac{3.9}{\sin 31^\circ}$$

$$b = \frac{3.9 \sin 101^\circ}{\sin 31^\circ} \quad \quad \quad b = \frac{3.9 \sin 17^\circ}{\sin 31^\circ}$$

$$b = 7.433\dots \quad \quad \quad b = 2.213\dots$$

In $\triangle ABC$, $b = 7.4$ cm, to the nearest tenth of a centimetre, and $\angle A = 48^\circ$ and $\angle B = 101^\circ$, both to the nearest degree, or
 $b = 2.2$ cm, to the nearest tenth of a centimetre, and $\angle A = 132^\circ$ and $\angle B = 17^\circ$, both to the nearest degree.

b)



$h = 20 \sin 43^\circ = 13.639\dots$
 Since this is less than 15 and less than 20, two solutions are possible, as shown in the diagram.

$$\frac{\sin P}{20} = \frac{\sin 43^\circ}{15}$$

$$\sin P = \frac{20 \sin 43^\circ}{15}$$

$$\angle P = \sin^{-1}\left(\frac{20 \sin 43^\circ}{15}\right)$$

$$\angle P = 65.413\dots$$

So $\angle P = 65^\circ$, or $\angle P = 180^\circ - 65^\circ = 115^\circ$.

Then, $\angle R = 180^\circ - (65^\circ + 43^\circ) = 72^\circ$, or $\angle R = 180^\circ - (115^\circ + 43^\circ) = 22^\circ$.

Now determine r for each value of $\angle R$:

$$\frac{r}{\sin 72^\circ} = \frac{15}{\sin 43^\circ} \quad \text{or} \quad \frac{r}{\sin 22^\circ} = \frac{15}{\sin 43^\circ}$$

$$r = \frac{15 \sin 72^\circ}{\sin 43^\circ}$$

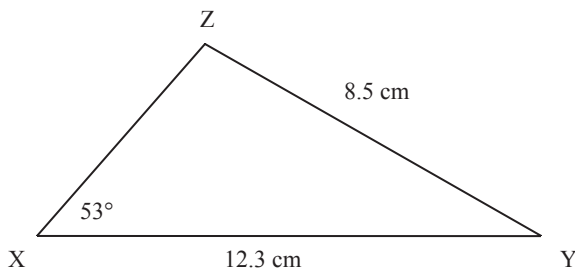
$$r = 20.917\dots$$

$$r = \frac{15 \sin 22^\circ}{\sin 43^\circ}$$

$$r = 8.239\dots$$

Therefore, in $\triangle PQR$, $\angle P = 65^\circ$, $\angle R = 72^\circ$, and $PQ = 20.9$ cm, or $\angle P = 115^\circ$, $\angle R = 22^\circ$, and $PQ = 8.2$ cm.

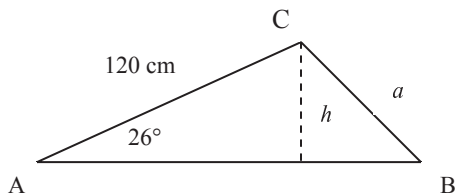
c)



$$h = 12.3 \sin 53^\circ = 9.823\dots$$

Since $8.5 < h$, no solution is possible.

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$$h = 120 \sin 26^\circ$$

$$h = 52.604\dots$$

a) There is one oblique triangle if $a \geq 120$ cm.