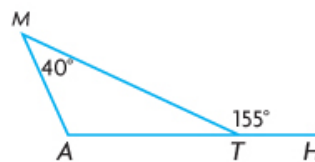


APPLY the Math

EXAMPLE 1 Using angle sums to determine angle measures

In the diagram, $\angle MTH$ is an **exterior angle** of $\triangle MAT$. Determine the measures of the unknown angles in $\triangle MAT$.



Serge's Solution

$$\begin{aligned}\angle MTA + \angle MTH &= 180^\circ \\ \angle MTA + (155^\circ) &= 180^\circ \\ \angle MTA &= 25^\circ\end{aligned}$$

$\angle MTA$ and $\angle MTH$ are supplementary since they form a straight line.

$$\begin{aligned}\angle MAT + \angle AMT + \angle MTA &= 180^\circ \\ \angle MAT + (40^\circ) + (25^\circ) &= 180^\circ \\ \angle MAT &= 115^\circ\end{aligned}$$

The sum of the measures of the interior angles of any triangle is 180° .

The measures of the unknown angles are:
 $\angle MTA = 25^\circ$; $\angle MAT = 115^\circ$.

Pull for Lesson Notes

EXAMPLE 2 Using reasoning to determine the relationship between the exterior and interior angles of a triangle

Determine the relationship between an exterior angle of a triangle and its **non-adjacent interior angles**.

Joanna's Solution



I drew a diagram of a triangle with one exterior angle. I labelled the angle measures a , b , c , and d .

$$\angle d + \angle c = 180^\circ$$

$$\angle d = 180^\circ - \angle c$$

$\angle d$ and $\angle c$ are supplementary. I rearranged these angles to isolate $\angle d$.

$$\angle a + \angle b + \angle c = 180^\circ$$

$$\angle a + \angle b = 180^\circ - \angle c$$

The sum of the measures of the angles in any triangle is 180° .

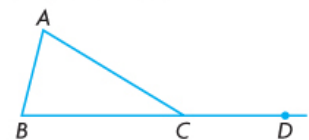
$$\angle d = \angle a + \angle b$$

Since $\angle d$ and $(\angle a + \angle b)$ are both equal to $180^\circ - \angle c$, by the transitive property, they must be equal to each other.

The measure of an exterior angle of a triangle is equal to the sum of the measures of the two non-adjacent interior angles.

non-adjacent interior angles

The two angles of a triangle that do not have the same vertex as an exterior angle.



$\angle A$ and $\angle B$ are non-adjacent interior angles to exterior $\angle ACD$.



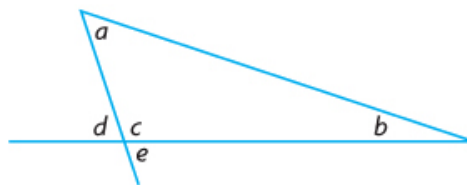
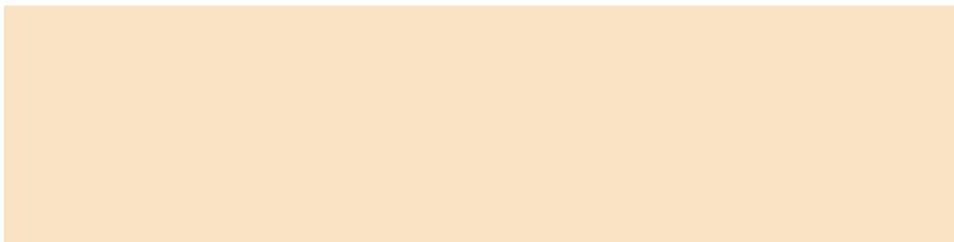
EXAMPLE 2

Using reasoning to determine the relationship between the exterior and interior angles of a triangle

Determine the relationship between an exterior angle of a triangle and its **non-adjacent interior angles**.

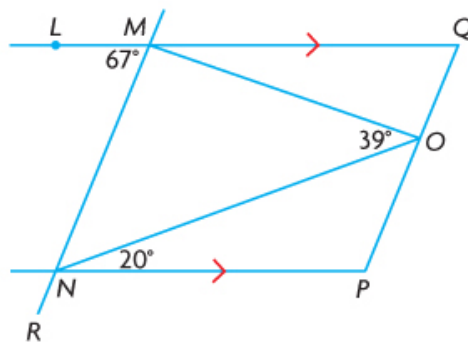
Your Turn

Prove: $\angle e = \angle a + \angle b$

**Answer**

EXAMPLE 3 Using reasoning to solve problems

Determine the measures of $\angle NMO$, $\angle MNO$, and $\angle QMO$.



Tyler's Solution

MN is a transversal of parallel lines LQ and NP .

MN intersects parallel lines LQ and NP .

$$\begin{aligned} \angle MNO + 20^\circ &= 67^\circ \\ \angle MNO &= 47^\circ \end{aligned}$$

Since $\angle LMN$ and $\angle MNP$ are alternate interior angles between parallel lines, they are equal.

$$\begin{aligned} \angle NMO + \angle MNO + 39^\circ &= 180^\circ \\ \angle NMO + (47^\circ) + 39^\circ &= 180^\circ \\ \angle NMO + 86^\circ &= 180^\circ \\ \angle NMO &= 94^\circ \end{aligned}$$

The measures of the angles in a triangle add to 180° .

$$\begin{aligned} \angle NMO + \angle QMO + 67^\circ &= 180^\circ \\ (94^\circ) + \angle QMO + 67^\circ &= 180^\circ \\ 161^\circ + \angle QMO &= 180^\circ \\ \angle QMO &= 19^\circ \end{aligned}$$

$\angle LMN$, $\angle NMO$, and $\angle QMO$ form a straight line, so their measures must add to 180° .

The measures of the angles are:

$$\angle MNO = 47^\circ; \angle NMO = 94^\circ; \angle QMO = 19^\circ.$$

SUMMARY

- In any triangle, the sum of the measure of the interior angles is proven to be 180° .
- The measure of any exterior angle of a triangle is proven to be equal to the sum of the measures of the two non-adjacent interior angles.

Attachments

PM11-2s3-2.gsp

2s3e2 finalt.mp4