

### 1.2.1 In Class or Homework Exercise

1. Convert 95.0 km/h into m/s.

$$95.0 \text{ km/h} \times \frac{1 \text{ m/s}}{3.6 \text{ km/h}} = \boxed{26.4 \text{ m/s}}$$

2. Convert 23.2 m/s into km/h.

$$23.2 \text{ m/s} \times \frac{3.6 \text{ km/h}}{1 \text{ m/s}} = \boxed{83.5 \text{ km/h}}$$

3. At an average speed of 11.8 km/h, how far will a bicyclist travel in 175 min?

$$v = 11.8 \text{ km/h}$$

$$t = 175 \text{ min} = 2.92 \text{ h}$$

$$\Delta d = ?$$

$$v = \frac{\Delta d}{t}$$

$$\Delta d = vt$$

$$= (11.8)(2.92)$$

$$= \boxed{34.5 \text{ km}}$$

4. If you average a speed of 45.0 km/h, how long will it take to travel a distance of 750 m?

$$v = 45.0 \text{ km/h} = 12.5 \text{ m/s}$$

$$\Delta d = 750 \text{ m}$$

$$t = ?$$

$$v = \frac{\Delta d}{t}$$

$$t = \frac{\Delta d}{v}$$

$$= \frac{750}{12.5}$$

$$= \boxed{60. \text{s}}$$

5. A confused person walks 5.0 km towards the east in 2.00 h, then 1.5 km towards the west in 0.50 h, and finally 10.0 km towards the east again in 2.25 h.

- a. What is the person's average speed?

$$\begin{array}{lll}
\Delta d_1 = 5.0\text{km} & \Delta d_t = \Delta d_1 + \Delta d_2 + \Delta d_3 & \\
\Delta d_2 = 1.5\text{km} & = 5.0 + 1.5 + 10.0 & v = \frac{\Delta d}{t} \\
\Delta d_3 = 10.0\text{km} & = 16.5\text{km} & = \frac{16.5}{4.75} \\
t_1 = 2.00\text{h} & & \\
t_2 = 0.50\text{h} & t_t = t_1 + t_2 + t_3 & = \boxed{3.47\text{ km/h}} \\
t_3 = 2.25\text{h} & = 2.00 + 0.50 + 2.25 & \\
v = ? & = 4.75\text{h} & 
\end{array}$$

b. What is the person's average velocity?

$$\begin{array}{lll}
\Delta \vec{d}_1 = 5.0\text{km} & \Delta \vec{d}_t = \Delta \vec{d}_1 + \Delta \vec{d}_2 + \Delta \vec{d}_3 & \\
\Delta \vec{d}_2 = -1.5\text{km} & = 5.0 + (-1.5) + 10.0 & \vec{v} = \frac{\Delta \vec{d}}{t} \\
\Delta \vec{d}_3 = 10.0\text{km} & = 13.5\text{km} & = \frac{13.5}{4.75} \\
t_1 = 2.00\text{h} & & \\
t_2 = 0.50\text{h} & t_t = t_1 + t_2 + t_3 & = \boxed{2.84\text{ km/h east}} \\
t_3 = 2.25\text{h} & = 2.00 + 0.50 + 2.25 & \\
\vec{v} = ? & = 4.75\text{h} & 
\end{array}$$

6. A person drove 4.0 km north, and then 6.4 km south.

a. If the person's average speed was 65 km/h, how long did the trip take?

$$\begin{array}{lll}
\Delta d_1 = 4.0\text{km} & \Delta d_t = \Delta d_1 + \Delta d_2 & v_t = \frac{\Delta d_t}{t_t} \\
\Delta d_2 = 6.4\text{km} & = 4.0 + 6.4 & \\
v_t = 65\text{km/h} & = 10.4\text{km} & 65 = \frac{10.4}{t_t} \\
t_t = ? & & t_t = \boxed{0.16\text{ h}}
\end{array}$$

b. What was the person's average velocity?

$$\begin{array}{lll}
\Delta \vec{d}_1 = 4.0\text{km} & \Delta \vec{d}_t = \Delta \vec{d}_1 + \Delta \vec{d}_2 & \vec{v}_t = \frac{\Delta \vec{d}_t}{t_t} \\
\Delta \vec{d}_2 = -6.4\text{km} & = 4.0 + (-6.4) & \\
t_t = 0.16\text{h} & = -2.4\text{km} & = \frac{-2.4}{0.16} \\
\vec{v}_t = ? & & = \boxed{-15\text{ km/h}}
\end{array}$$

The average velocity is 15 km/h south.

7. A rock thrown horizontally at a large bell 50.0 m away is heard to hit the bell 4.50 s later. If the speed of sound is 330 m/s, what was the speed of the rock?

This problem can be broken up into 2 parts, the rock moving and the sound coming back. Since we know more about the sound, start with that:

**Sound**

$$\Delta d_s = 50.0\text{ m}$$

$$v_s = 330\text{ m/s}$$

$$t_s = ?$$

$$v_s = \frac{\Delta d_s}{t_s}$$

$$t_s = \frac{\Delta d_s}{v_s}$$

$$= \frac{50.0}{330}$$

$$= 0.15\text{ s}$$

**Rock**

$$\Delta d_r = 50.0\text{ m}$$

$$t_r = 4.50 - 0.15\text{ s} = 4.35\text{ s}$$

$$v_r = ?$$

$$v_r = \frac{\Delta d_r}{t_r}$$

$$= \frac{50.0}{4.35}$$

$$= \boxed{11.5\text{ m/s}}$$

8. A person starts from home and drives with a velocity of 55 km/h east for 30 minutes. They then drive with a velocity of 73 km/h west for 45 minutes. Where are they?

**Part 1**

$$\vec{v}_1 = 55\text{ km/h}$$

$$t_1 = 30.\text{ min} = 0.50\text{ h}$$

$$\Delta \vec{d}_1 = ?$$

$$\vec{v}_1 = \frac{\Delta \vec{d}_1}{t_1}$$

$$55 = \frac{\Delta \vec{d}_1}{0.50}$$

$$\Delta \vec{d}_1 = 27.5\text{ km}$$

**Part 2**

$$\vec{v}_2 = -73\text{ km/h}$$

$$t_2 = 45\text{ min} = 0.75\text{ h}$$

$$\Delta \vec{d}_2 = ?$$

$$\vec{v}_2 = \frac{\Delta \vec{d}_2}{t_2}$$

$$-73 = \frac{\Delta \vec{d}_2}{0.75}$$

$$\Delta \vec{d}_2 = -54.8\text{ km}$$

**Total**

$$\Delta \vec{d}_T = \Delta \vec{d}_1 + \Delta \vec{d}_2$$

$$= 27.5 + (-54.8)$$

$$= -27.3\text{ km}$$

$$= \boxed{-27\text{ km}}$$

The person is 27 km west of their starting point.

9. Two people start at the same location. One person jogs with a velocity of 3.5 m/s east; the other person jogs with a velocity of 1.5 m/s west. How far apart are they after 8.2 s?

**Person 1**

$$\vec{v}_1 = 3.5 \text{ m/s}$$

$$t_1 = 8.2 \text{ s}$$

$$\Delta \vec{d}_1 = ?$$

**Person 2**

$$\vec{v}_2 = -1.5 \text{ m/s}$$

$$t_2 = 8.2 \text{ s}$$

$$\Delta \vec{d}_2 = ?$$

$$\vec{v}_1 = \frac{\Delta \vec{d}_1}{t_1}$$

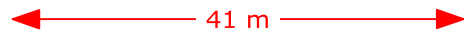
$$3.5 = \frac{\Delta \vec{d}_1}{8.2}$$

$$\Delta \vec{d}_1 = 29 \text{ m}$$

$$\vec{v}_2 = \frac{\Delta \vec{d}_2}{t_2}$$

$$-1.5 = \frac{\Delta \vec{d}_2}{8.2}$$

$$\Delta \vec{d}_2 = -12 \text{ m}$$



As can be seen, the two people will be 41m apart.

10. You drive a car 2.0 h at 40. km/h, then 2.0 h at 60. km/h.  
a. What is your average speed?

**Part 1**

$$v_1 = 40. \text{ km/h}$$

$$t_1 = 2.0 \text{ h}$$

$$\Delta d_1 = ?$$

**Part 2**

$$v_2 = 60. \text{ km/h}$$

$$t_2 = 2.0 \text{ h}$$

$$\Delta d_2 = ?$$

**Total**

$$\Delta d_t = 200 \text{ km}$$

$$v_t = ?$$

$$t_t = 4.0 \text{ h}$$

$$v_1 = \frac{\Delta d_1}{t_1}$$

$$40. = \frac{\Delta d_1}{2.0}$$

$$\Delta d_1 = 80. \text{ km}$$

$$v_2 = \frac{\Delta d_2}{t_2}$$

$$60. = \frac{\Delta d_2}{2.0}$$

$$\Delta d_2 = 120. \text{ km}$$

$$v_t = \frac{\Delta d_t}{t_t}$$

$$= \frac{200}{4.0}$$

$$= \boxed{50. \text{ km/h}}$$

Notice that in this case the average speed actually is the same as the answer that would be obtained by averaging the two speeds together; **this is only because the time spent at each speed was equal.**

- b. Do you get the same answer if you drive 100 km at each of the two speeds above (equal distances instead of equal times)?

**Part 1**

$$v_1 = 40. \text{ km/h}$$

$$t_1 = ?$$

$$\Delta d_1 = 100 \text{ km}$$

**Part 2**

$$v_2 = 60. \text{ km/h}$$

$$t_2 = ?$$

$$\Delta d_2 = 100 \text{ km}$$

**Total**

$$\Delta d_t = 200 \text{ km}$$

$$v_t = ?$$

$$t_t = 4.17 \text{ h}$$

$$\begin{array}{lll}
 v_1 = \frac{\Delta d_1}{t_1} & v_2 = \frac{\Delta d_2}{t_2} & v_t = \frac{\Delta d_t}{t_t} \\
 40. = \frac{100}{t_1} & 60. = \frac{100}{t_2} & = \frac{200}{4.17} \\
 t_1 = 2.5h & t_2 = 1.67h & = \boxed{48 \text{ km/h}}
 \end{array}$$

No, you do not obtain the same answer since different times were spent at each speed.

11. You plan a 200. km trip on which you want to average a speed of 90. km/h. You cover the first half of the distance at an average speed of only 48 km/h. What must your average speed be in the second half of the trip to meet your goal?

**Total**

$$\begin{array}{l}
 \Delta d_t = 200. \text{ km} \\
 v_t = 90. \text{ km/h} \\
 t_t = ?
 \end{array}$$

**Part 1**

$$\begin{array}{l}
 v_1 = 48 \text{ km/h} \\
 \Delta d_1 = 100. \text{ km} \\
 t_1 = ?
 \end{array}$$

**Part 2**

$$\begin{array}{l}
 t_2 = 2.22 - 2.08 = 0.14h \\
 \Delta d_2 = 100. \text{ km} \\
 v_2 = ?
 \end{array}$$

$$\begin{array}{l}
 v_t = \frac{\Delta d_t}{t_t} \\
 90. = \frac{200.}{t_t} \\
 t_t = 2.22h
 \end{array}$$

$$\begin{array}{l}
 v_1 = \frac{\Delta d_1}{t_1} \\
 48 = \frac{100.}{t_1} \\
 t_1 = 2.08h
 \end{array}$$

$$\begin{array}{l}
 v_2 = \frac{\Delta d_2}{t_2} \\
 = \frac{100.}{0.14} \\
 = \boxed{710 \text{ km/h}}
 \end{array}$$

Obviously, it would not be possible to meet the goal of an average speed of 90 km/h, since almost all of the time was used up in the first part of the race.

12. A biker rides around a track twice. The track has a radius of 70.0 m. The first trip around the track is completed in 26.8 s, while the second lap takes 32.4 s.
- a. What is the average speed of the biker?

Since the radius of the track is given, the circumference of the track must be calculated:

$$\begin{array}{l}
 C = 2\pi r \\
 = 2\pi(70.0) \\
 = 440. \text{ m}
 \end{array}$$

$$\begin{aligned}\Delta d_i &= 880.m \\ t_i &= 59.2 s \\ v &= ?\end{aligned}\quad \begin{aligned}v &= \frac{\Delta d}{t} \\ &= \frac{880.}{59.2} \\ &= \boxed{14.9 m/s}\end{aligned}$$

b. What is the average velocity of the biker?

Since the biker is going around a circular track, he returns to his starting point and therefore has a displacement of zero.

$$\begin{aligned}\vec{v} &= \frac{\Delta \vec{d}}{t} \\ &= \frac{0}{59.2} \\ &= \boxed{0 km/h}\end{aligned}$$